# BCA $6{ }^{\text {TH }}$ Semester (Honours) Examination, 2021 <br> BACHELOR OF COMPUTER APPLICATION <br> Course ID: <br> Course Code: BCA-601 <br> Course Title: Theory of Computation <br> Full Marks: 80 <br> Time: 4 Hr <br> The figure in the margin indicate full marks. Candidates are required to give their answers in their own words as far as practicable. 

## Group: A

1. Answer all the questions:
i. A shift register is a :
a. Mealy $\mathrm{m} / \mathrm{c}$
b. Moore $\mathrm{m} / \mathrm{c}$
c. Turing $\mathrm{m} / \mathrm{c}$
d. All of the above
e. None of the above.
ii. DFA has:
a. Single final sate
b. More than one initial states
c. Unique path to the final state
d. All of the above.
e. None of the above
iii. A regular language over an alphabet $\Sigma$ is one that can't be obtained from the basic language using the operation $\qquad$
a. Union
b. Concatenation
c. Kleene*
d. All of the above
e. None of the above
iv. Which one is true of the following?
a. Merger graph is a directed graph
b. Compatible graph is a directed graph
c. Both are directed graph
d. Merger graph has Unique path to the final state
e. None of the above
v. A grammar with more than one parse tree is called $\qquad$
a. Unambiguous
b. Ambiguous
c. Regular
d. NPDA
e. None of the above
vi. In FSM diagram what does circle represent?
a. Change of states
b. States
c. $O / P$ value
d. Initial State
e. None of the above
vii. If $L_{1}$ and $L_{2}$ are context free language, which of the following is true?
a. $\mathrm{L}_{1}$ *
b. $\mathrm{L}_{2} \mathrm{UL}_{1}$
c. $\mathrm{L}_{1} . \mathrm{L}_{2}$
d. All of the above
e. None of the above
viii. Regular Expression $x / y$ denotes the set $\qquad$
a. $\{x, y\}$
b. $\{x y\}$
c. $\{x\}$
d. $\{y\}$
e. None of the above
ix. Which of the following strings is not generated by the following grammar? $\mathrm{S} \rightarrow \mathrm{SaSbS} \mid \varepsilon$
a. aabb
b. abab
c. aababb
d. aaabbb
e. None of the above
x. Number of states requires to accept strings with length of 3 $\qquad$
a. 3
b. 4
c. 5
d. Can't be represented
e. None of the above.

## Group: B

2. Answer any Ten questions:
i. Define DFA.
ii. What do you mean by unit production?
iii. What is language?
iv. Regular languages are all context free- Justify.
v. What do you mean by acceptability of a string? Explain.
vi. What are the operations for regular expression?
vii. What is Mealy machine?
viii. What do you mean by right linear grammar?
ix. What do you mean by $\sum^{*}$ ?
$x$. Define complement of a language.
xi. Define error state in the context of FA.
xii. Define synchronous sequential circuit.
xiii. What is Grammar?
xiv. Define NPDA.
$x v . \quad L=\{a, a a, a a a, a a b, \ldots .$.$\} over \sum\{a, b\}$. Is it possible to design a DFA for $L$ ? Explain.

## Group: C

3. Answer any Four questions:
i. State Pumping lemma for regular language.
ii. Show that the Union of two context free language is context free.
iii. Design a PDA for the language $L=\left\{w w^{R}: w \in\{0,1\}^{*}\right\}$.
iv. Prove that $L=\left\{a^{P}: P\right.$ is prime $\}$ over $\sum\{a\}$ is not regular.
v. What is the basic difference between Mealy and Moore machine? Construct a Mealy machine which is equivalent to the Moore machine given below:

| PS | $\mathrm{X}=0$ | $\mathrm{X}=1$ | Z |
| :--- | :--- | :--- | :--- |
| $\mathrm{q}_{0}$ | q 1 | q 2 | 1 |
| $\mathrm{q}_{1}$ | $\mathrm{q}_{3}$ | $\mathrm{q}_{2}$ | 0 |
| $\mathrm{q}_{2}$ | q 2 | $\mathrm{q}_{1}$ | 1 |
| $\mathrm{q}_{3}$ | q 0 | $\mathrm{q}_{3}$ | 1 |

vi. Let $G$ be the grammar $S \rightarrow a B|b a, A \rightarrow a| a S|b A A, B \rightarrow b| b S \mid a B B$, for the string aaabbabbba find.
a. Left most derivation
b. Right most derivation
c. Parse tree

## Group: D

4. Answer any Three questions:

10X3=30
i. Draw the merger graph, merger table, compatibility graph and then minimize the following machine:

| PS | $\mathrm{I}_{0}$ | $\mathrm{I}_{1}$ | $\mathrm{I}_{2}$ | $\mathrm{I}_{3}$ |
| :--- | :--- | :--- | :--- | :--- |
| A | - | $\mathrm{C}, 1$ | $\mathrm{E}, 1$ | $\mathrm{~B}, 1$ |
| B | $\mathrm{E}, 0$ | - | - | - |
| C | $\mathrm{F}, 0$ | $\mathrm{~F}, 1$ | - | $\mathrm{B}, 1$ |
| D | - | - | $\mathrm{B}, 1$ | - |
| E | - | $\mathrm{F}, 0$ | $\mathrm{~A}, 0$ | $\mathrm{D},-$ |
| F | $\mathrm{C}_{-}$ | - | $\mathrm{B}, 0$ | $\mathrm{C}, 1$ |

ii. a. State the difference between DFA \& NFA.
b. Design a DFA which accepts set of all binary string contains 1100 or 1010 as substrings.
c. Construct a regular expression corresponding to the state diagram describe by following figure:
$2+3+5$

iii. a. Construct PDA accepting the set of all string over $\{a, b\}$ with equal number of a's \& b's.
b. Using Pumping Lemma prove that the set $L=\left\{0^{i} 1^{i} \mid i>1\right\}$ is not regular.
iv. a. Construct the minimum state automata equivalent to given automata defined below: ( ${ }^{*} q_{2}$ indicate that $q_{2}$ is the final state )

| $P S$ | $a$ | $b$ |
| :--- | :--- | :--- |
| $\rightarrow q_{0}$ | $q_{5}$ | $q_{1}$ |
| $q_{1}$ | $q_{2}$ | $q_{6}$ |
| ${ }^{*} q_{2}$ | $q_{2}$ | $q_{0}$ |
| $q_{4}$ | $q_{5}$ | $q_{7}$ |
| $q_{5}$ | $q_{6}$ | $q_{2}$ |
| $q_{6}$ | $q_{4}$ | $q_{6}$ |
| $q_{7}$ | $q_{2}$ | $q_{6}$ |

b. Convert the following NFA to DFA:

v. a. What do you mean by a sub tree of a derivation tree?
b. Write the CFG for the language $L=\left\{0^{i} 1^{j} 2^{k} \mid i=j\right.$ or $\left.j=k\right\}$
$2+5+3$
c. $\mathrm{E} \rightarrow \mathrm{E}+\mathrm{E}\left|\mathrm{E}^{*} \mathrm{E}\right|$ a. Prove that the CFG with this production rule is ambiguous.
vi. a. A long sequence of input pluses enters a two input, two output synchronous sequential circuit, which is required a produced an output $Z=1$, whenever a sequence 010101 occurs, overlapping sequence are accepted. Draw the state transition diagram.
b. Define inverse machine.

